One way to characterize students’ representations is to distinguish between concrete, semi-concrete, semi-abstract and abstract representations. In a previous study with 6-year olds we surprisingly found that – while solving a combinatorial task - the children who used semi-concrete representations in their documentations were more systematic in the process of finding solutions with less duplications than the children who used semi-abstract representations. As a continuation, we have provided 6-year olds with a specially designed application focused on combinatorial task. The aim of the application is to provide an opportunity to develop an understanding of combinatorics and its systematisation by letting children work within the semi-concrete level. The first results of the study indicate that the children indeed develop significant skills when working within the semi-concrete level, for instance they seem to have obtained a good understanding of what the concept different combinations entails.

Keywords: Abstraction, combinatorics, representations.

Short description of the research topic and theoretical framework

The focus of this poster is on the links between representations and solutions when 6-year-olds work on combinatorial tasks. The task can be explained as follows: In how many ways can three bears sit on a sofa?

Studies of young children’s representations often focus on informal and formal representations. Abstraction is often perceived as a goal and teachers often value when young children use abstract representations. Heddens (1986) introduced semi-concrete and semi-abstract as connections between concrete (objects) and abstract (signs) representations. He referred to representations of real situations, for example, pictures of real items, as semi-concrete, whereas he referred to symbolic representations of concrete items, where the symbols or pictures do not look like the objects they represent, as semi-abstract. Connected to the task presented above, concrete implies real bears and a sofa, semi-concrete implies images of (resembling) bears, semi-abstract implies a symbolic, not resembling, representation of the bears and abstract implies the use of formal signs. As for the concrete level, the ‘real’ bears can be replaced by three play-bears, or by engaging in a role-play, enacting the situation. In both semi-concrete and semi-abstract representations, the colours of the bears and their symbols are often kept identical.

When conducting the exercise in 13 pre-school classes in Sweden (125 children, age 6), children showed different levels of abstraction in their solutions of the problem. In a previous paper we problematized the apparent relation between the level of abstraction and the number of duplicate
solutions. Surprisingly we found that the children who used semi-concrete representations in their
documentations made more systematically solutions with less duplication than the children who
used semi-abstract representations. We argued that a more abstract level seemed to reduce the
problem from bears on a sofa to putting three coloured dots on a paper. It seemed that children
moved too fast to the next level of abstraction. Internalisation of the problem had not occurred yet
which led to a reduction of the problem as described above. Simultaneously, we also concluded that
documentation within the semi-concrete level was very time-consuming for children, as it takes a lot
of time for the children to draw bears (Palmér & van Bommel, in press).

Methodology

How could we slow down these children without slowing down the process of documentation? An
application was especially designed to let children work on the semi-concrete level, and
simultaneously, the time-consuming issue of drawing the bears was taken into account. The design-
principles for the application concerned a possibility to adjust the level of the problem, resulting in a
choice of the number of bears and the size of sofa. It also resulted in the possibility to save solutions
as well as to offer an insight to all outcomes. By doing so, we wanted to explore the semi-concrete
level more explicitly and focus on the learning opportunities this level of abstraction can offer the
children.

During autumn of 2016, 6-year-olds (about 60) from different preschool-classes have tested the
application. Our reflections concern the learning opportunities created by using the digital form of
documentation (in addition to the paper and pencil forms). After using the application, we let the
children work on similar combinatorial tasks but only by using paper and pencil.

Preliminary results

Our preliminary results show that the children who have worked with the application do not
document as many duplicates when using semi-abstract representations as the children in our
previous study (Palmér & van Bommel, in press). Additionally, we see an increase in the systematic
way they organise and search for solutions. A special note has to be made towards the possibility to
adjust the level of the exercise in the application. For example, some children explored the
situations of two bears on a three-seat sofa and four-seat sofas with different number of bears. Such
explorations led to discussions of similarities between two and three bears on a three-seat sofa and
mathematical aspects of the tasks were discussed at another level compared to paper and pencil
lessons.

References

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